

***Cognitively Guided Instruction:  
A Selection of Publications  
November 2010  
Compiled by Linda Levi, Teachers Development Group***

This is a selection of published work related to Cognitively Guided Instruction. Other sources can be found by looking for other work by these authors and in the reference list of these publications.

Alexander, C. & Ambrose, R. (August 2010). Digesting student-authored story problems. *Mathematics Teaching in the Middle School*, 16, (1), 27-33.

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Ambrose, R. & Kenehan, G. (2009). Children's Evolving Understanding of Polyhedra in the Classroom, *Mathematical Thinking and Learning*, Vol 11 (3), 158 - 176.

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Battey, D. & Franke, M. L. (2008). Transforming identities: Understanding teachers across professional development and classroom practice. *Teacher Education Quarterly*, 35(3), 127-149.

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Blogs run by members of the CGI team:

Empson, Susan B. *Learning Math, Teaching Math* by at <http://www.edb.utexas.edu/empson/>

Levi, Linda L. *Understanding Children's Mathematic* at <http://www.lindalevi@blogspot.com>

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